

# Carrier-envelope phase shift caused by variation of grating separation

Chengquan Li, Eric Moon, and Zenghu Chang

*J. R. Macdonald Laboratory, Department of Physics, Kansas State University, Manhattan, Kansas 66506*

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The effects of variation of the grating separation in a stretcher on the carrier-envelope (CE) phase of amplified pulses are investigated. By translating one of the telescope mirrors in the stretcher with a piezoelectric transducer, it is found that a  $1\ \mu\text{m}$  change of the distance causes a  $3.7 \pm 1.2$  rad shift of the CE phase, which is consistent with theoretical estimations. The results indicate that optical mounts used for gratings and telescope mirrors must be interferometrically stable; otherwise their vibration and thermal drift will cause significant phase error. The CE phase drift was corrected by feedback controlling the grating separation. © 2006 Optical Society of America

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Chirped pulse amplification is a well-developed technique for generating high-power laser pulses with durations longer than 10 fs.<sup>1</sup> The pulses from the chirped pulse amplifier can be compressed to  $\sim 5$  fs with  $\sim 1$  mJ of energy at an  $\sim 750$  nm center wavelength. For such intense, few-cycle pulses, it is crucial to control their carrier-envelope (CE) phase for strong-field atomic physics studies.<sup>2</sup> In this Letter we focus on the effects of the stability of the grating separation in the stretcher and compressor on the CE phase variation, which have been overlooked so far.

The experiments were done by using the Kansas Light Source laser system, as shown in Fig. 1.<sup>3</sup> The CE offset frequency,  $f_0$ , of the chirped-mirror-based femtosecond oscillator (Femtosecond Pro) was locked to a quarter of the oscillator repetition rate (80 MHz). This was done by measuring  $f_0$  with a Mach-Zehnder-type  $f$ -to- $2f$  interferometer. The signal was used to feedback control the power from the pump laser<sup>4</sup> (Coherent Verdi 6). The pulses with the same CE phase were selected by a Pockels cell and sent to the stretcher of the chirped pulse amplifier with a repetition rate of 1 kHz. The pulses with an  $\sim 100$  nm bandwidth and 3 nJ of energy were stretched to  $\sim 80$  ps. Then the stretched pulses were amplified to 5 mJ with a 14-pass amplifier. The Ti:sapphire crystal was cooled to liquid-nitrogen temperature to reduce the thermal lens effect. After amplification, the pulses were compressed by a pair of gratings to 2.5 mJ and 25 fs. A fraction of the output beam ( $< 1\ \mu\text{J}$ ) was used to measure the relative CE phase of the amplified pulses with a collinear  $f$ -to- $2f$  interferometer.<sup>5</sup> Compared with material- and prism-based stretchers and compressors, the grating-based stretcher and compressor are important for producing higher-energy pulses. Thus, understanding the effects of the stretcher and compressor on the CE phase has attracted a lot of attention.<sup>5-7</sup>

The stretcher configuration in our laser system is shown in Fig. 2(a). It uses mirrors for the telescope to avoid chromatic aberrations. The analysis given here can also be applied to a stretcher with a lens-based telescope as shown in Fig. 2(b). In the frequency do-

main, the input electric field can be expressed as  $E(\omega) = E_0(\omega) \exp\{i[\varphi_{\text{CE}} + \phi(\omega)]\}$ , where  $|E_0(\omega)|^2$  is the power spectrum and  $\varphi_{\text{CE}}$  is the CE phase. The spectral phase is given by  $\phi(\omega)$ , which is equal to zero when the input pulses are transform limited as assumed here.

When the pulse propagates through the double-pass grating stretcher, its spectral phase becomes<sup>8,9</sup>

$$\phi'(\omega) = \omega\tau(\omega) - 4\pi(G_s/d_s)\tan[\gamma_s - \theta_s(\omega)], \quad (1)$$

where  $\omega$  represents the frequency components of the pulse,  $\tau$  is the group delay,  $G_s$  is the effective perpendicular distance between the gratings,  $d_s$  is the grating constant,  $\gamma_s$  is the angle of incidence, and  $\theta_s$  is the acute angle between the incident and the diffracted rays, which is positive when the incidence angle is larger than the diffraction angle.

The CE phase change is caused by the shift of electric field oscillation with respect to the pulse envelope.

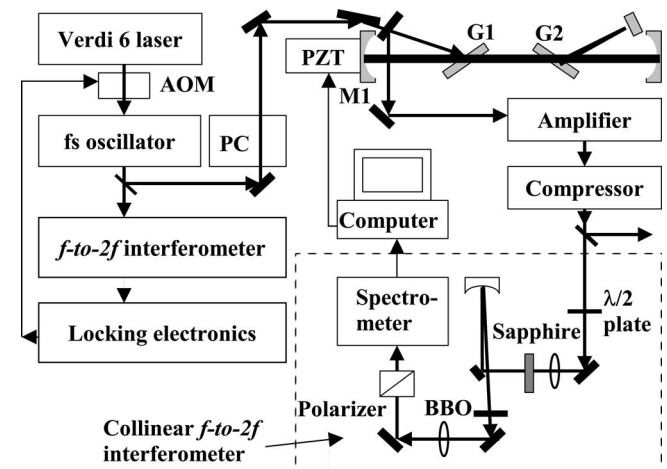


Fig. 1. Kansas Light Source laser system for testing the effects of the grating separation of the stretcher on the CE phase stability. G1 and G2 are the gratings. M1 is one of the telescope mirrors driven by a piezoelectric transducer (PZT). The oscillator CE offset frequency  $f_0$  is stabilized by feedback controlling the acousto-optic modulator (AOM). Pulses with the same CE phase are selected by the Pockels cell (PC) and are sent to the chirped pulse amplifier.

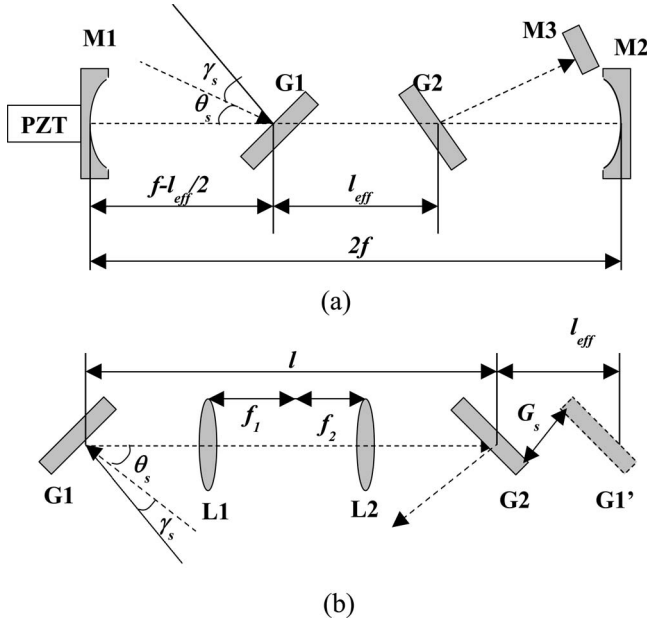


Fig. 2. Parameters of the grating stretcher. Mirrors are used in (a) to form the telescope. G1 and G2 are the gratings;  $\gamma_s$  is the incidence angle on the first grating;  $\theta_s$  is the angle between the diffracted beam and the incident beam; M1 and M2 are mirrors for the telescope;  $l_{\text{eff}}$  is the effective distance. (b) Conventional stretcher with a lens-based telescope. G1' is the image of the G1 formed by the telescope.  $G_s$  is the effective perpendicular distance between the gratings.

lope. As is shown in Ref. 8, the carrier wave oscillation of the output pulse at the observation plane is described by the phase given in Eq. (1) at  $\omega_0$ , whereas the group delay that represents the time for the envelope to propagate through the stretcher is  $\tau(\omega_0)$ , which is the derivative of the phase with respect to frequency evaluated at  $\omega_0$ . To compare the carrier wave oscillation with the envelope in phase space, we can rewrite the group delay in  $\omega_0\tau(\omega_0)$ . Thus, the CE phase change is  $\omega_0\tau(\omega_0) - \phi'(\omega_0)$ , which yields

$$\begin{aligned} \phi'_{\text{CE}} - \phi_{\text{CE}} &= \omega_0\tau(\omega_0) - \phi'(\omega_0) \\ &= 4\pi(G_s/d_s)\tan[\gamma_s - \theta_s(\omega)]. \end{aligned} \quad (2)$$

In the previous expression,  $\phi'_{\text{CE}}$  is the CE phase at the exit and  $\omega_0$  is the carrier frequency. The variation of  $\gamma_s$  due to laser beam pointing stability can change  $\phi'_{\text{CE}}$ , which has been studied before.<sup>5,6</sup> In a double-pass configuration, the net effect of the incident angle variation on the CE phase is small. Equation (2) is also valid for grating compressors. The only difference is the sign of  $G_s$ .

Since  $G_s = -l_{\text{eff}}\cos(\gamma_s - \theta_s)$ ,<sup>9</sup> the amount of CE phase error introduced by the variation of the effective linear grating separation,  $\Delta l_{\text{eff}}$ , is  $\Delta\phi_{\text{CE}} = -4\pi\sin(\gamma_s - \theta_s)\Delta l_{\text{eff}}/d_s$ . The change of the value of  $l_{\text{eff}}$  can originate from the motion of either the lenses or the gratings. For most stretcher and compressor designs, the incident angle is close to the Littrow angle  $\gamma_l$ , i.e.,  $\theta_s = 0^\circ$  and  $\sin(\gamma_l) = \lambda/(2d_s)$ . Considering the gratings having  $d_s \approx \lambda$ , the CE phase shift is given by

$$\frac{\Delta\phi_{\text{CE}}}{\Delta l_{\text{eff}}} = 2\pi\frac{\lambda}{d_s^2} \approx \frac{2\pi}{\lambda}. \quad (3)$$

The analysis reveals that the CE phase change is significant when the variation of the linear separation of the gratings is of the order of the laser wavelength. On the other hand, the compressed pulse duration does not change much when  $\Delta l_{\text{eff}} \approx \lambda$ . This is because

$$(\tau'_p)^2 = \tau_p^2 + \left(\frac{\tau_s}{l_{\text{eff}}}\Delta l_{\text{eff}}\right)^2, \quad (4)$$

where  $\tau'_p$  is the compressed pulse duration with the varied grating separation and  $\tau_s$  is the stretched pulse duration. For our laser,  $\tau_p \approx 20$  fs,  $\tau_s/l_{\text{eff}} \approx 1$  fs/ $\mu\text{m}$ ; changing the grating separation by an amount of the order of the laser wavelength can cause an increase of only a fraction of a femtosecond in laser pulse duration. Thus, for CE phase stabilized amplifiers, the requirement for mechanical stability is much stricter than for conventional chirped pulse amplification.

To measure the phase shift caused by the variation of  $l_{\text{eff}}$ , we introduced a small change  $\Delta l_{\text{eff}}$  by moving mirror M1. When M1 moves away from G1 by an amount  $\Delta$ , it can be shown with the imaging equations that the change of  $l_{\text{eff}}$  is

$$\Delta l_{\text{eff}} = -\Delta - (l_{\text{eff}}/2f)^2\Delta. \quad (5)$$

The first term is from the increase of the distance between the first grating to the first mirror, while the second term originates from the increase of the mirror separation. Since  $l_{\text{eff}} < 2f$ , the contribution from the latter is small, which can be neglected for our stretcher. Thus the CE phase shift is given by

$$\frac{\Delta\phi_{\text{CE}}}{\Delta} \approx \frac{\Delta\phi_{\text{CE}}}{\Delta l_{\text{eff}}} = 4\pi\sin(\gamma_s - \theta_s)\frac{1}{d_s}. \quad (6)$$

For our stretcher, the groove density of the two ruled gratings is  $1/d_s = 1200$  lines/mm. The focal length of the two telescope mirrors is  $f = 250$  mm. When the two mirrors are confocal, the effective linear distance between the gratings is  $l_{\text{eff}} = 130$  mm. This is the distance between the second grating and the image of the first grating. The incident angle of the beam on the first grating, G1, is  $\gamma_s = 33.5^\circ$ , and the diffraction angle is  $(\gamma_s - \theta_s) = 23.3^\circ$ . Using these parameters, it was estimated that  $\Delta\phi_{\text{CE}}/\Delta \approx 6$  rad/ $\mu\text{m}$ .

The dependence of CE phase on the grating separation was measured experimentally by driving one of the telescope mirrors with a PZT stage. M1 was chosen because of its small size. When a sinusoidal wave with 60 V peak-to-peak amplitude was applied to the PZT, it moved back and forth with a 3.6  $\mu\text{m}$  displacement amplitude. The measured CE phase variation is shown in Figs. 3(a) and 3(c). As a reference, Figs. 3(b) and 3(d) are the measured CE phase of the amplified pulses when a dc voltage was applied. It was deduced from the results shown in Fig. 3(c) that  $\Delta\phi_{\text{CE}}/\Delta \approx \Delta\phi_{\text{CE}}/\Delta l_{\text{eff}} \approx 3.7 \pm 1.2$  rad/ $\mu\text{m}$ ,

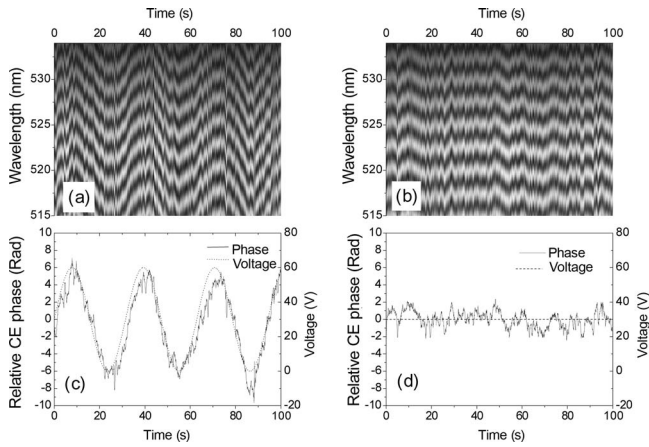


Fig. 3. Dependence of the CE phase of the amplified pulses on the grating separation. (a), (c) Fringe pattern of the collinear  $f$ -to- $2f$  interferometer and the corresponding relative CE phase obtained when a 60 V sinusoidal voltage is applied to the PZT, which caused the PZT to move  $3.6 \mu\text{m}$ ; (b), (d) with a 30 V dc voltage applied to the PZT.

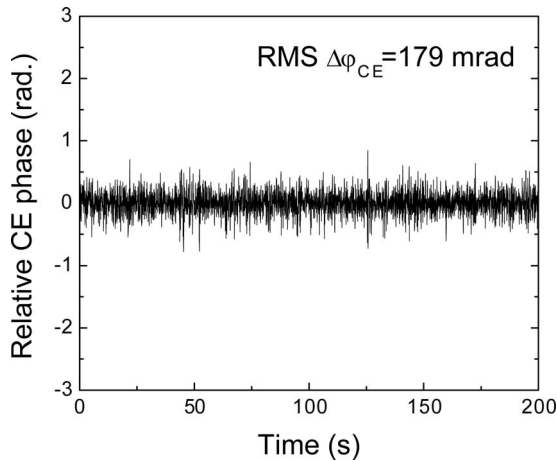


Fig. 4. CE phase of the amplified pulses stabilized by feedback controlling the grating separation. The rms phase error in 200 s is 179 mrad. The CE phase drift without the stabilization is shown in Fig. 3(d).

which agreed with the calculated results within a factor of 2. The origin of the discrepancy and large error is from the PZT uncertainty ( $6.1 \pm 1.5 \mu\text{m}/100 \text{ V}$ ) and from the random drift of the CE phase. The results demonstrate that a subwavelength change of the grating separation can indeed cause significant CE phase variation. Since the gratings in the stretchers and compressor are not interferometrically stable, their vibration and thermal drift contribute to the variation of the CE phase in Fig. 3(d). Previously, the slow CE phase drift introduced by the chirped pulse amplifier was precompensated by adding a feedback loop to the oscillator  $f_0$  locking electronics, using the measured CE phase from the collinear  $f$ -to- $2f$  as the

input.<sup>2</sup> We chose to feedback control the grating separation in the stretcher, instead. There are two advantages to our method. First, it does not disturb the oscillator, which should yield a more stable output power from the oscillator because of reduced pump power modulation. Second, the feedback bandwidth is not limited by the channel of the oscillator locking electronics for the slow feedback. The relative CE phase with the feedback control is shown in Fig. 4. The RMS phase error is 179 mrad over 3 min. This can be improved further in the future.

In conclusion, it was found that the carrier-envelope (CE) phase of the pulses from a chirped pulse amplifier with 1 kHz repetition rate is susceptible to variation of the grating separation in the stretchers and compressors, which can be estimated by a simple expression  $\Delta\varphi_{\text{CE}}/\Delta l_{\text{eff}} \approx 2\pi/\lambda$ . For our stretcher, the measured value is  $\Delta\varphi_{\text{CE}}/\Delta l_{\text{eff}} \approx 3.7 \pm 1.2 \text{ rad}/\mu\text{m}$ , which is close to the calculated value ( $6 \text{ rad}/\mu\text{m}$ ). We demonstrated that the CE phase of the amplified pulses can be stabilized to 179 mrad by feedback controlling the grating separation in the stretcher. The effects of the mismatch of repetition rates between the oscillator and the amplifier on the CE phase were studied in Ref. 10.

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