

# OPTICAL MODELING OF THE INTERNAL BACK REFLECTANCE OF VARIOUS C-SI DIELECTRIC STACKS FEATURING $\text{AlO}_x$ , $\text{SiN}_x$ , $\text{TiO}_2$ AND $\text{SiO}_2$

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## ABSTRACT

One promising path to a reduced cost of crystalline silicon (c-Si) photovoltaics (PV) is to increase silicon usage efficiency by using thinner wafers. Many challenges arise when transitioning to thin wafer cells, including increased surface recombination at the rear side of the cell, increased wafer bowing, and a reduction in optical absorption due to a decreased optical path length within the silicon. Rear side passivation provides great promise in addressing these challenges. This paper addresses rear side dielectric configurations that can optimize back surface reflectance, in addition to providing excellent surface passivation. Optical modeling of various stack configurations is examined to explore the back surface reflectance at the Si-dielectric interface for different film combinations and thicknesses as a function of wavelength and internal angle of incidence. Specifically, configurations using aluminum oxide ( $\text{AlO}_x$ ), silicon nitride ( $\text{SiN}_x$ ), titanium dioxide ( $\text{TiO}_2$ ), and silicon dioxide ( $\text{SiO}_2$ ) were investigated with a focus on designing stack configurations that will also allow for high quality passivation and are compatible with a high-volume manufacturing environment.

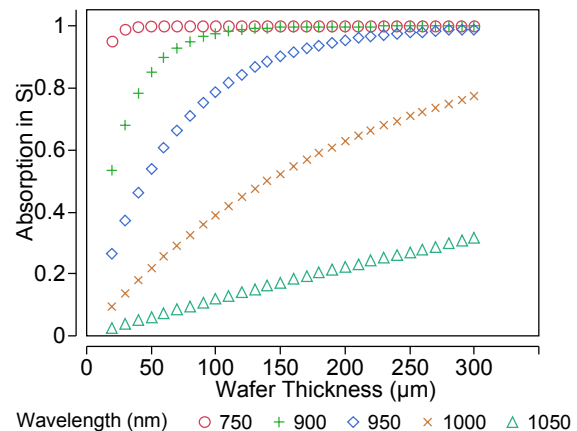
## INTRODUCTION

A large portion of the cost of a final c-Si PV module is due to the silicon used to create the solar cells [1]. Thin wafers (e.g. < 150  $\mu\text{m}$ ) have received much attention due to the potential to significantly reduce module cost [2-4]. There are still many challenges associated with processing thin silicon wafers including: wafer handling [5]; wafer bowing when using a full Al back contact [6]; surface recombination at the back side of the cell [7]; and reduced absorption of near-bandgap photons [8].

In-line deposition of rear side dielectric passivation layers has emerged as a strong candidate to realize PERC-type solar cells, which address the issues of wafer bowing and rear side surface recombination. This paper focuses on modeling the optical properties of various single and double layer dielectric stack configurations, with particular attention to the backside internal reflectance at the Si-dielectric interface.

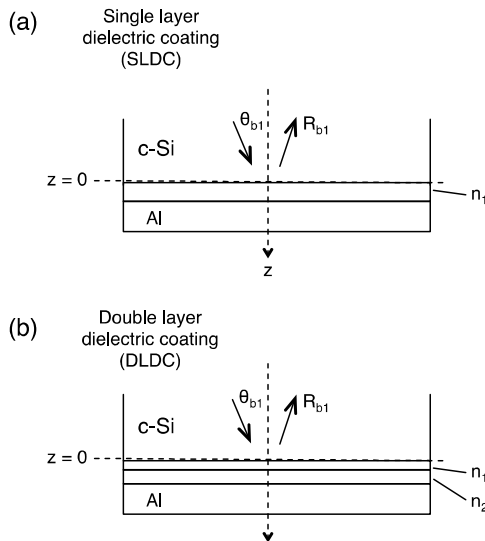
In particular, various layer combinations and thicknesses are investigated with the intent to optimize the internal back reflectance (BR) for near bandgap photons. Higher

reflectance effectively increases the optical path length of the cell, which can lead to increased absorption, particularly at longer wavelengths, which are poorly absorbed in c-Si due to the indirect bandgap. This is highlighted in Fig. 1 where the fraction of light absorbed in c-Si as a function of wafer thickness is given for five wavelengths between 750 nm - 1050 nm using published extinction coefficients [9].



**Figure 1:** Optical absorption in c-Si as a function of wafer thickness for five different wavelengths between 750 nm - 1050 nm, calculated using published extinction coefficient data for Si [9].

$\text{AlO}_x$  has gained significant attention as a rear side passivation material for p-type solar cells. Surface recombination velocities below 13 cm/s have been achieved with this material, and it possesses many advantages over other materials [10]. In an industrial PERC cell design, the thin  $\text{AlO}_x$  film will likely require a capping layer to prevent the screen printed Al paste from penetrating through the  $\text{AlO}_x$ , and the capping layer should add little cost. Therefore, dielectric stack configurations using  $\text{AlO}_x$  have recently been explored experimentally, including  $\text{AlO}_x\text{-SiN}_x$  and  $\text{AlO}_x\text{-SiO}_2$  [11,12]. The dielectric stack configurations considered in this simulation study all consist of an  $\text{AlO}_x$  passivation layer of at least 10 nm thick to ensure compatibility with well designed p-type PERC cells, in terms of effective chemical and field effect passivation (Fig. 2). A single  $\text{AlO}_x$  layer is used as a reference case. Additionally, stacks featuring  $\text{SiN}_x$ ,  $\text{TiO}_2$  and  $\text{SiO}_2$  capping layers are investigated.



**Figure 2:** Dielectric stack configurations simulated in this study: (a) single layer dielectric coating and (b) double layer dielectric coating ( $\text{AlO}_x\text{-TiO}_2$ ,  $\text{AlO}_x\text{-SiO}_2$ ,  $\text{AlO}_x\text{-SiN}_x$ ).

## METHODOLOGY

Much of the previous work related to characterizing the internal BR of c-Si solar cells has relied on the utilization of experimentally measured internal quantum efficiency (IQE) and calculating the aggregate BR over all relevant wavelengths using raytracing software and solar cell simulation tools, such as RAYN and SUNRAYS [13]. In addition, much of this work has focused on  $\text{SiO}_2$  and  $\text{SiN}_x$  film stacks.

This simulation study has been carried out by first directly simulating the internal BR, irrespective of the cell electronic properties, similar to the treatment by Green [14], but expanded to include multiple materials and stack configurations and different frontside optics (e.g. with and without encapsulation). Here the relative internal BR is calculated for various wavelengths ( $\lambda$ ), angles of incidence between the silicon and initial dielectric layer ( $\theta_{b1}$ ) and various dielectric configurations (both in terms of material combinations and thicknesses). The goal is to provide new insight and a starting point for comparing the various dielectric configurations.

The transfer matrix method [15] of calculating multilayer transmission/reflectance using optical admittances of each medium is used to determine internal BR as a function of layer thickness for the different stack configurations at four near-bandgap wavelengths (900 nm, 950 nm, 1000 nm, 1050 nm) and as a function of  $\theta_{b1}$ . In this treatment, the dielectric layers are assumed to be lossless ( $k = 0$ ), and the assumed values are given in Table 1, taken from both the literature [9,16] and our spectroscopic ellipsometry measurements carried out on films deposited by atmospheric pressure chemical vapor deposition (APCVD)

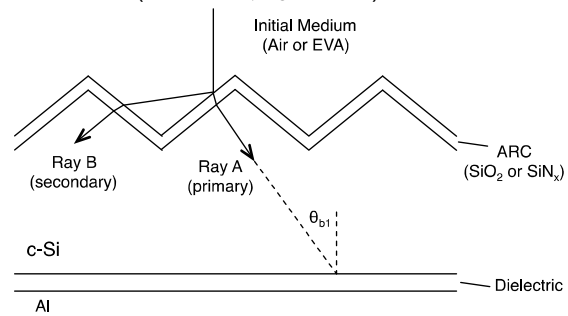
and plasma-enhanced CVD. For the Si and Al layers, the complex refractive index parameters are used throughout the calculations to account for losses due to the evanescent wave occurring for angles beyond the critical angle ( $\theta_c$ ). This last point is crucial, since the critical angle between Si and  $\text{AlO}_x$  is  $\approx 26.5^\circ$  ( $n_{\text{AlO}_x} = 1.6$ ,  $\lambda = 1000$  nm), and the angle of incidence of most of the radiation on the backside is larger than this. This means the surface wave and evanescent losses are the dominant loss mechanisms for internal BR with these types of cell configurations.

Dielectric Layer	Refractive Index
$\text{AlO}_x$	1.60
$\text{SiO}_2$	1.46
$\text{TiO}_2$	2.00
$\text{SiN}_x$ (unencapsulated)	2.06
$\text{SiN}_x$ (encapsulated)	2.20

**Table 1:** Assumed refractive index values for dielectrics

\* It should be noted that the refractive index of  $\text{TiO}_2$  changes significantly depending on process conditions.

For textured monocrystalline wafers, the characteristic base angle ( $\alpha$ ) of the well-known pyramid structures is commonly taken to be  $54.74^\circ$ , although recent work has shown that in industrial cells this is actually around  $50\text{-}52^\circ$  depending on the etchant used [17]. Assuming  $\alpha = 54.74^\circ$  and a  $\text{SiO}_2$  frontside coating, Kray *et al.* show that at normal incidence, the two primary rays transmitted through the cell have an angle of incidence (AOI) on the backside of  $41.4^\circ$  and  $59.1^\circ$ , the former (Ray A) being the primary ray, which carries 76.4% of the total incident flux and the latter (Ray B) carrying 19.4% [13]. This is illustrated in Fig. 3. Using simple geometrical optics equations, one can show that the primary ray for a similar cell with a  $\text{SiN}_x$  anti-reflection coating (ARC) has an equivalent backside AOI. However, the backside AOI of the primary ray for an encapsulated cell is significantly lower at  $\approx 35^\circ$  ( $n_{\text{EVA}} = 1.5$ ,  $n_{\text{SiN}_x} = 2.2$ ).

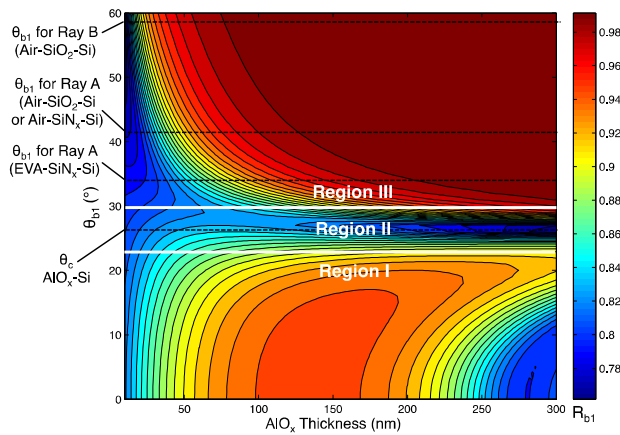


**Figure 3:** Schematic illustrating two primary transmitted rays in a textured monocrystalline solar cell (from Reference 13). Note: the backside AOI of the primary ray for an encapsulated cell is smaller ( $35^\circ$ ) than that of an unencapsulated cell ( $41.4^\circ$ ).

## RESULTS AND DISCUSSION

By plotting contour maps of the internal BR vs. dielectric layer thickness and  $\theta_{b1}$ , some interesting trends can be seen. For example, there are three critical regions in terms of the backside AOI, as shown in Fig. 4.

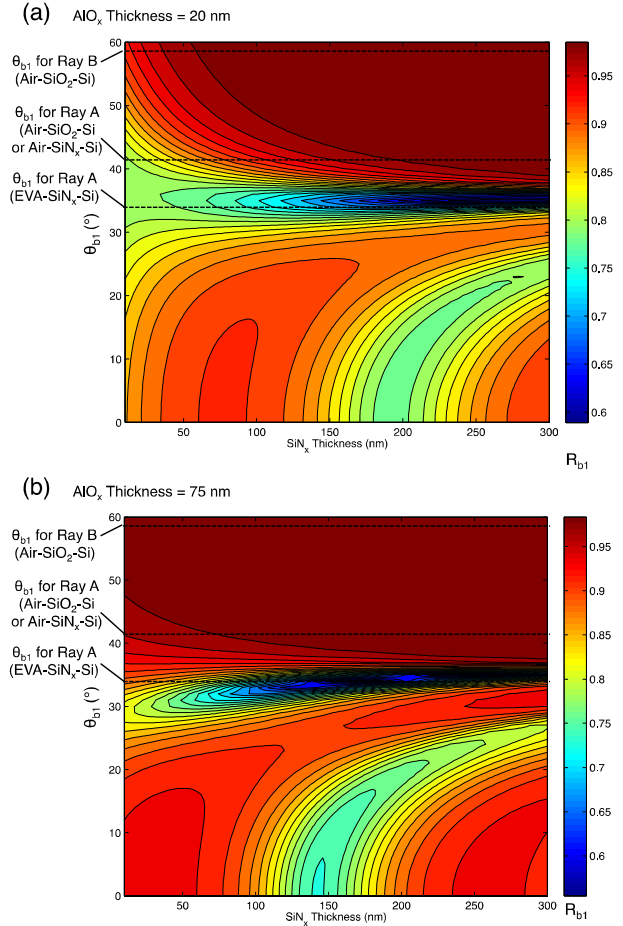
- Region I ( $\theta_{b1} < \theta_c$ ): In this region, interference effects play a key role, hence the periodic dependence on layer thickness (constructive vs. destructive interference). These angles are less interesting for anisotropically etched monocrystalline cells, due to the light scattering of the primary beams, but could be of interest in cells with different texturing and ARC configurations (e.g. black silicon).
- Region II ( $\theta_{b1}$  near  $\theta_c$ ): This region features significant losses due to the surface wave propagating along the Si-AIO<sub>x</sub> interface, allowing for more energy transfer to the lossy Al layer.
- Region III ( $\theta_{b1} > \theta_c$ ): Above the critical angle, a thicker dielectric layer means higher internal BR due to the further separation from the Al layer.



**Figure 4:** Internal BR contour map for rearside SLDC with AIO<sub>x</sub>, highlighting the three regions of interest and  $\theta_{b1}$  values for primary rays of cells with and without encapsulation.

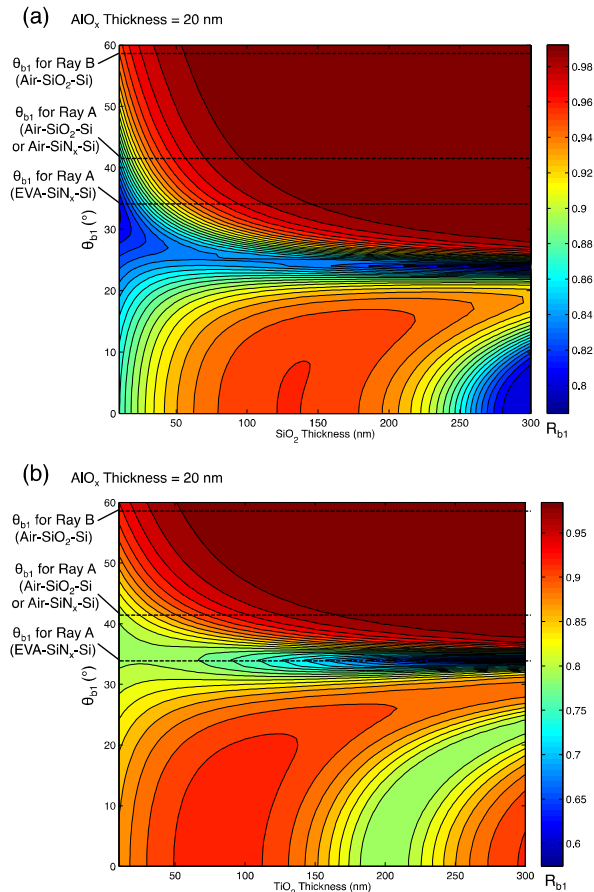
In this case of a SLDC with AIO<sub>x</sub>, the primary rays for cells with and without encapsulation fall within Region III. Therefore, layer thickness isn't very critical, as long as it is beyond a certain thickness. Based on cost considerations, the AIO<sub>x</sub> film thickness should be limited. As mentioned before for an industrial PERC cell, a lower cost capping layer should be used to prevent the screen printed Al paste from penetrating through the AIO<sub>x</sub>. Fig. 5 shows results for a SiN<sub>x</sub> capping layer with two different AIO<sub>x</sub> thicknesses (20 nm, 75 nm).

In this case, due to the higher index of refraction of SiN<sub>x</sub> compared to AIO<sub>x</sub>, the poorly reflecting Region II is effectively shifted to higher values of  $\theta_{b1}$ . While this doesn't significantly affect the unencapsulated cell case, it could reduce the internal BR for encapsulated cells, which have a smaller  $\theta_{b1}$ .



**Figure 5:** Internal BR contour maps for rearside DLDC with AIO<sub>x</sub>-SiN<sub>x</sub> as a function of SiN<sub>x</sub> thickness and  $\theta_{b1}$  for two fixed AIO<sub>x</sub> thicknesses: (a) 20 nm and (b) 75 nm. The  $\theta_{b1}$  values for primary rays are also included.

Results for DLDC configurations with TiO<sub>2</sub> and SiO<sub>2</sub> capping layers have also been included (amorphous TiO<sub>2</sub> with a refractive index of 2.0 assumed), both with a fixed AIO<sub>x</sub> thickness of 20 nm (Fig. 6). The lower refractive index of SiO<sub>2</sub> ensures that Region II is suppressed to values below that of the  $\theta_{b1}$  values for the primary rays of interest. The amorphous TiO<sub>2</sub> is found to be almost identical to that of the SiN<sub>x</sub> results due to the similar refractive index values.



**Figure 6:** Internal BR contour maps for rearside DLDC with (a)  $\text{AlO}_x\text{-SiO}_2$  and (b)  $\text{AlO}_x\text{-TiO}_2$ .

## CONCLUSION

In conclusion, the internal back reflectance has been modeled as a function of dielectric layer thickness and the backside angle of incidence at the Si-dielectric interface. Single and double layer dielectric rearside coatings have been considered, using  $\text{AlO}_x$ ,  $\text{SiN}_x$ ,  $\text{TiO}_2$  and  $\text{SiO}_2$ . The results clearly show the three critical regions, in terms of backside angle of incidence, for these configurations:  $\theta_{b1} < \theta_c$ ;  $\theta_{b1}$  near  $\theta_c$ ; and  $\theta_{b1} > \theta_c$ . For DLDC configurations with a thicker second layer, the second region (near  $\theta_c$ ) is shifted to either higher angles of incidence (for  $\text{SiN}_x$  and  $\text{TiO}_2$ ) or lower angles (for  $\text{SiO}_2$ ). This affect could play an important role in the internal back reflectance of encapsulated cells with rearside dielectric configurations.

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